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Introduction to Surface Acoustic Wave (SAW) Devices

Part 4: Resonator-Based RF Filters

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- Basic Filter Design
- Ladder Type Filter Design
- Lattice Filter Design
- Stacked Resonator Filter Design
- Coupled Resonator Filter Design

Contents

• Basic Filter Design

N-th Order Butterworth Filter

Maximally Flat Response: $H^{(n)}(0)=0$ for $n=1,2,\dots N$



Gradual Skirt & Group Delay Characteristics

N-th Order Chebyshev Filter



7 Element T-type Butterworth LPF





•Original LPF (Cut-off ω_c) •LPF to HPF $\omega_c C'_1 = 1/\omega_c L_1$ $\omega_c L'_2 = 1/\omega_c C_2$ •LPF to BPF $\omega_0^2 L'_1 C'_1 = 1, \ \omega_0^2 L'_2 C'_2 = 1$ $(\omega_0 + \omega_c)L'_1 - 1/(\omega_0 + \omega_c)C'_1 = \omega_c L_1$ $(\omega_0 + \omega_c)C'_2 - 1/(\omega_0 + \omega_c)L'_2 = \omega_c C_2$

•LPF to BEF $\omega_0^2 L'_1 C'_1 = 1, \ \omega_0^2 L'_2 C'_2 = 1$ $(\omega_0 + \omega_c) C'_1 - 1/(\omega_0 + \omega_c) L'_1 = 1/\omega_c L_1$ $(\omega_0 + \omega_c) L'_2 - 1/(\omega_0 + \omega_c) C'_2 = 1/\omega_c C_2$



Infinite Q

Q=100 for Parallel-L

Q=100 for Series-L



Increased Insertion Loss

Influence of Mutual L



$$V_{1} = L_{1} \frac{dI_{1}}{dt} + M \frac{dI_{2}}{dt} = (L_{1} - M) \frac{dI_{1}}{dt} + M \frac{d}{dt} (I_{1} + I_{2})$$
$$V_{2} = M \frac{dI_{1}}{dt} + L_{2} \frac{dI_{2}}{dt} = (L_{2} - M) \frac{dI_{2}}{dt} + M \frac{d}{dt} (I_{1} + I_{2})$$





Uniform Impedance Values

Cascade-Connection with Inversion

(Equivalent Circuit for Transmission Line)



Similar Response to Butterworth Filter



Interference Between Two Reflected Waves



100% Transmit When $L=n\lambda/2$







$$\mathbf{F} = \begin{cases} \begin{bmatrix} \xi^{-1} \cosh M\varphi & Z_i \xi \sinh M\varphi \\ Z_i^{-1} \xi \sinh M\varphi & \xi \cosh M\varphi \end{bmatrix} & (M: \text{odd}) \\ \begin{bmatrix} \cosh M\varphi & Z_i \sinh M\varphi \\ Z_i^{-1} \sinh M\varphi & \cosh M\varphi \end{bmatrix} & (M: \text{even}) \end{cases}$$



$$S_{21} = \frac{2}{F_{11} + F_{22} + R_0 F_{21} + G_0 F_{12}}$$

$$= \begin{cases} \frac{2}{(\xi + \xi^{-1}) \cosh M\varphi + (Z_i \xi^{-1} / R_0 + R_0 \xi / Z_i) \sinh M\varphi} & (M: \text{odd}) \\ \frac{2}{2 \cosh M\varphi + (Z_i / R_0 + R_0 / Z_i) \sinh M\varphi} & (M: \text{even}) \end{cases}$$

When $\varphi = jn\pi / M$, $|S_{21}|=1$



When $\omega < \omega_c$, φ Imag., $Z_i \& Z_o$ Real \Rightarrow Passband

When $\omega > \omega_c$, φ Real, $Z_i \& Z_o$ Imag. \Rightarrow Rejection band

Zero Insertion Loss $\varphi = jn\pi/M \Rightarrow \omega/\omega_c = sin(n\pi/M)$





Steep Skirt and Good Out-Band Rejection

Contents

• Ladder Type Filter Design

Ladder-Type Filter



Configuration (Resonator-Based Constant K Filter)

- Fabrication of Multiple Resonators on a Chip
- Low Loss
- High Power Durability
- Moderate Out-of-Band Rejection

Performance of Ladder-Type SAW Filter



Fujitsu FAR-F6CP-2G1400-L21M

W-CDMA-Rx







Resonator Model for Y_p & Y_s

$$Y = j\omega C_0 \frac{(j\omega/\omega_a)^2 + 1 + (j\omega/\omega_a)/Q_r}{(j\omega/\omega_r)^2 + 1 + (j\omega/\omega_r)/Q_r}$$

Assumption 1. $\gamma \& Q_r$ Identical for $Z_s \& Z_p$

2. $\omega_r^{s} = \omega_a^{p}$





Passband When $-1 < Y_p/Y_s < 0$ (Either Y_s or Y_p Inductive)



Passband When $-1 < Y_p/Y_s < 0$ (Either Y_s or Y_p Inductive) Larger Y_s Offers Wide Bandwidth

$$S_{21} = \begin{cases} \frac{2}{(\xi + \xi^{-1}) \cosh M\varphi + (Z_i \xi^{-1} / R_0 + R_0 \xi / Z_i) \sinh M\varphi} & (M : \text{odd}) \\ \frac{2}{2 \cosh M\varphi + (Z_i / R_0 + R_0 / Z_i) \sinh M\varphi} & (M : \text{even}) \end{cases}$$

At the Resonance(
$$\varphi=0$$
)
 $S_{21}|_{\omega=\omega_r^s} \cong \frac{2}{2+N(Z_s/R_0+R_0/Z_p)}$ where $\eta = R_0 \omega \sqrt{C_0^s C_0^p}$
 $r = \sqrt{C_0^p/C_0^s}$
 $M = Q_r/\gamma$ (FOM)

Loss Minimum Condition η=1

$$S_{21}\Big|_{\substack{\omega=\omega_r^s\\\eta=1}} \cong \frac{1}{1+NrM^{-1}}$$

Low Loss When NrM⁻¹«1

Bandwidth

$$\frac{2\delta\omega}{\omega_r^s} \cong \sqrt{1 + \frac{1}{\sqrt{\gamma(1+\gamma)(1+r^2)}}} - \sqrt{1 - \frac{1}{\sqrt{\gamma(1+\gamma)(1+r^2)}}}$$
$$\cong \frac{1}{\sqrt{\gamma(1+\gamma)(1+r^2)}} \cong \frac{1}{\gamma\sqrt{1+r^2}} \quad \text{where } r = \sqrt{C_0^p / C_0^s}$$

Out-of-Band Rejection

When
$$\eta = 1$$
, $S_{21} \cong \frac{1}{\cosh(N\varphi)} = \frac{1}{T_N(\sqrt{r^2 + 1})}$

where $T_N(x) = \cosh(N\cosh^{-1}x)$: Chebyshev Polynomial

N Influences IL and OoB Rejection

r Influences IL, Bandwidth and OoB Rejection













Influence of Common Impedance



Equivalent Circuit





Design of Ladder-type Filters

- Resonator γ Limits Achievable Band Width
- For IL Minimization, $\omega_r^2 C_0^p C_0^s R_s^2 \approx 1$
- For Wide bandwidth, $\omega_r^{\ s}$ should be a little larger than $\omega_a^{\ p}$
- With smaller $r = \sqrt{C_0^p / C_0^s}$, IL and Band Width Improved but OoB Rejection Deteriorated.
- With N, OoB Rejection Improved but IL Increases
- *IL* is Very Sensitive to Motional Resistance of Y_s
- Very Sensitive to Parasitics
- Q Influences IL and Shoulder Characteristics



• Lattice Filter Design





Modified Equivalent Circuit

Equivalent to 2-Stage Cascaded L-type (or π -type) Filter



Resonance ConditionRes. Freq. for
$$Y_o$$
Res. Freq. for Y_e IOrIAnti-Res. Freq. for Y_e Anti-Res. Freq. for Y_o $S_{21} = \frac{R_0(Y_o - Y_e)}{(1 + Y_e R_0)(1 + Y_o R_0)}$

At Resonance

$$S_{21}|_{\omega=\omega_r^o} \cong \frac{\eta(M^{-1}-M)}{\eta^2 + \eta(M^{-1}+M) + 1} \quad \text{Where } M = Q_r/\gamma, \ \eta = \omega C_0 R_0$$

IL Min. Condition $\eta=1 \implies S_{21}|_{\omega=\omega_r^o} \cong \frac{1-M}{1+M}$



Good OoB Rejection

Wideband When $\omega_r^{o} > \omega_a^{e}$



Better OoB Rejection When $C_0^{o} > C_0^{e}$



Null Generation Near Passband



$$S_{21} = \frac{R_0(Y_o - Y_e)}{(1 + Y_e R_0)(1 + Y_o R_0)}$$

Null Generation When $Y_e = Y_o$

Influence of Mutual Coupling



Very Small Values but May Not Negligible



Tiny Coupling Gives Significant Influence



• Stacked Resonator Filter Design



Static Capacitance When Parallel-Connected

1-Port Resonator When Parallel-Connected with Inversion



$$\frac{i_{1}}{e_{1}} + \frac{L_{m}}{C_{0}} + \frac{R_{m}}{C_{0}} + \frac{i_{2}}{e_{2}}$$

$$\frac{i_{1}}{e_{1}} + \frac{L_{m}}{C_{0}} + \frac{R_{m}}{C_{0}} + \frac{i_{2}}{e_{2}}$$

$$\frac{i_{1}}{e_{2}} + \frac{I_{11}}{E_{2}} + \frac$$

$$Z \approx 2j(\omega - \omega_{0})L + R_{m} + \frac{2j\omega_{0}C_{0}R_{0}^{2}}{1 + (\omega_{0}C_{0}R_{0})^{2}} \text{ Gives}$$

$$S_{21} \approx \frac{G_{0}}{(G_{0} + j\omega C_{0})^{2}[j(\omega - \omega_{0})L + R_{m}/2 + G_{0}/\{G_{0}^{2} + (\omega C_{0})^{2}\}]}$$

$$|S_{21}|_{\omega = \omega_{0}} \approx \frac{1}{R_{m}\{1 + (\omega_{0}C_{0}R_{0})^{2}\}/2R_{0} + 1}}$$

$$IL \text{ Min. Condition } \omega_{0}C_{0}R_{0} = 1$$

$$Q = \frac{1}{\omega_{0}C_{m}R_{m}} = \frac{\omega_{0}L_{m}}{R_{m}}$$

$$M = Q/\gamma$$

Determined by M

When
$$\omega_0 C_0 = G_0$$
 $S_{21} \approx \frac{1}{j[2j\gamma(\omega - \omega_0)/\omega_0 + M^{-1} + 1]}$

When $\omega = \omega_{\pm} = \omega_0 [1 \pm \gamma^{-1} (1 + M^{-1})/2] \qquad |S_{21}| \approx \frac{1}{\sqrt{2}} \frac{1}{[1 + M^{-1}]}$

-3dB Bandwidth

$$\frac{\omega_{+}-\omega_{-}}{\omega_{0}} = \gamma^{-1}(1+M^{-1})$$

$$\implies |S_{21}|_{\omega=\omega_0} \bullet \frac{\omega_+ - \omega_-}{\omega_0} \approx \gamma^{-1}$$

$$\gamma = C_0 / C_m$$
$$Q = \frac{1}{\omega_0 C_m R_m} = \frac{\omega_0 L_m}{R_m}$$
$$M = Q / \gamma$$

Determined by M and γ

Response of Stacked Resonator Filter



ZnO ($L=1.6 \mu m$, $S=160 \times 160 \mu m^2$) S is Set to Z-Match at 2GHz

Cascaded Stacked Resonator Filters







• Coupled Resonator Filter Design



Resonance Frequency: $\omega_r = (k/M)^{0.5}$



Resonance Frequency

Symmetric Resonance: $\omega_{rs} = \{(k+2k_c)/M\}^{0.5}$

Antisymmetric Resonance: $\omega_{ra} = (k/M)^{0.5}$

Coupled Resonator



(a) Electric + Mechanical Circuit



(a) Electric + Mechanical Circuit



(b) Mechanical Circuit



(a) Symmetric Resonance



(b) Antisymmetric Resonance







Equivalent to Lattice Filter



Design Principle of Wideband DMS Filters

Coincidence of Multiple Resonance ω for Y_e (or Y_o) with Antiresonance ω for Y_o (or Y_e)



Employing More Resonances Results in More Bandwidths

Double Mode SAW (DMS) Filter



Fujitsu FAR-F5EB-942M50-B28E

Coupled Resonator Filter (CRF)





Cascaded CRF

ZnO (*L*=1.6 μm, *S*=220×220 μm²)

Coupler 2 GRayls, 0.18 λ Extremely hard

ZnO (*L*=1.6 μm, *S*=160×160 μm²)

Coupler 1 MRayls, 0.1 λ Extremely soft

Design of Coupled Resonator Filters

- Band Width Governed by γ
- For Loss Minimization, $\omega_r C_0 R_s \approx 1$
- Coupling Layer Should be Designed to Adjust Multiple Poles to Coincide with Nulls (But Very Critical!)
- Slight Difference Between Poles & Nulls Effective
- Cascade-Connection is Effective
- IL is Sensitive to Motional Resistances & Parasitics